Ecography

## ECOG-05281

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Supplementary material

## Appendix 1

## **Supplementary Text**

Derivation of a distance-based conspecific-encounter index

To effectively incorporate distance information of sequentially sampled neighboring organisms, inspired from the unification of the original index v and Moran's I index (see Eqs. 1-4 in the main text), we develop a distance-based conspecific-encounter index as follows:

$$v_d = \frac{\sum_{i \in S} \sum_{k \ge 2} e^{-d_{k,k-1}} I(Z_k = Z_{k-1} = i)}{\sum_{k \ge 2} e^{-d_{k,k-1}}},$$
(A1)

where  $d_{k,k-1}$  denotes the distance between the k-th and (k-1)-th organisms. One important purpose of introducing the denominator  $\sum_{k\geq 2} e^{-d_{k,k-1}}$  in Eq. A1 is to normalize the distance-based index to make it bounded between 0 and 1. When  $d_{2,1}=d_{3,2}=\cdots=d_{m,m-1}$ , the above equation actually is identical to the original conspecific-encounter index v. Another important consideration of formulating the distance-based index  $v_d$  as Eq. A1 above is because it could have a similar relationship with Moran's I index as proved below.

Firstly, like the partitioning of the original index v into species-specific components (Eq. 1 in the main text), we can also partition the above distance-based index  $v_d$  into separated components for different species (i.e., species-specific distance-based index  $v_d(i)$ ) found within the sampling line transect as

$$v_d = \sum_{i \in S} v_d(i)$$
.

Here,

$$v_d(i) = \frac{\sum_{k \ge 2} e^{-d_{k,k-1}} I(Z_k = Z_{k-1} = i)}{\sum_{k \ge 2} e^{-d_{k,k-1}}}.$$

For Moran's I index with a specific species i, we have

$$I_d(i) = \left(\frac{m}{\sum_{k=1}^m q_k}\right) \left(\frac{\sum_{k=1}^m \sum_{j=1}^m w_{k,j} q_k q_j}{\sum_{k=1}^m \sum_{j=1}^m w_{k,j}}\right),\tag{A2}$$

where we let  $q_k = I(Z_k = i)$  and  $w_{k,j} = e^{-d_{k,j}}$  for |k-j| = 1 and  $w_{k,j} = 0$  otherwise. Clearly, we have  $\sum_{k=1}^m \sum_{j=1}^m w_{k,j} = 2 \sum_{k \geq 2} e^{-d_{k,k-1}}$  and  $\sum_{k=1}^m \sum_{j=1}^m w_{k,j} q_k q_j = 2 \sum_{k \geq 2} e^{-d_{k,k-1}} I(Z_k = Z_{k-1} = i)$ . Moreover,  $n_i = \sum_{k=1}^m q_k$  is the observed abundance of species i within the line transect.

Consequently, we obtain a simple relationship between the species-specific Moran's I index and the species-specific distance-based  $v_d$  index as

$$I_d(i) = \left(\frac{m}{n_i}\right) v_d(i).$$

As such, when conducting line-transect sampling, the distance-based conspecific-encounter index  $v_d$  can be computed as the sum of abundance-weighted Moran's I index for each single species along the line transect as follows:

$$v_d = \sum_{i \in S} \left(\frac{n_i}{m}\right) I_d(i). \tag{A3}$$

This distance-based conspecific-encounter index is an extension of the original index but effectively accounts for the potential influence of spatial distance when measuring multi-species distributional aggregation level for line-transect sampling.

Derivation of a functional conspecific-encounter index

We define the functional conspecific-encounter index as

$$v_F = \frac{\sum_{i \in S} \sum_{k \ge 2} I(Z_k = Z_{k-1} = i) e^{-|X_k - X_{k-1}|}}{\sum_{k \ge 2} e^{-|X_k - X_{k-1}|}},$$
(A4)

where  $X_k$  is the value of the targeted functional trait of the k-th encountered organism along a line transect. The denominator  $\sum_{k\geq 2} e^{-|X_k-X_{k-1}|}$  in the index  $v_F$  is to normalize the index to have a range between 0 and 1; moreover, it stands for the functional trait difference between sequentially encountered neighboring organisms, irrespective of their species-level identity. The introduction of the indicator function  $I(Z_k = Z_{k-1} = i)$  in the numerator confines the index  $v_F$  to focus on the functional trait distance or difference between two sequentially encountered organisms from the same species. If all  $X_k$ 's are the same or missing, the functional conspecific-encounter index  $v_F$  is identical to the original index v.

Being analogous to the partition of the original conspecific-encounter index into species-specific components presented in the main text, we can partition the index  $v_F$  into species-specific components as

$$v_F = \sum_{i \in S} v_F(i).$$

Here,

$$v_F(i) = \frac{\sum_{k \ge 2} I(Z_k = Z_{k-1} = i) e^{-|X_k - X_{k-1}|}}{\sum_{k > 2} e^{-|X_k - X_{k-1}|}}.$$

For the form of the species-specific Moran's I index, the calculation formula again follows Eq. A2 (or Eq. 2 in the main text). However, for the functional conspecific-encounter index here,

the weight is different: we set  $q_k = I(Z_k = i)$  and  $w_{k,j} = e^{-|X_k - X_j|}$  for |k - j| = 1 and  $w_{k,j} = 0$  otherwise. Then, we have  $\sum_{k=1}^m \sum_{j=1}^m w_{k,j} = 2 \sum_{k \ge 2} e^{-|X_k - X_{k-1}|}$  and  $\sum_{k=1}^m \sum_{j=1}^m w_{k,j} q_k q_j = 2 \sum_{k \ge 2} e^{-|X_k - X_{k-1}|} I(Z_k = Z_{k-1} = i)$ . Again,  $n_i = \sum_{k=1}^m q_k$  represents the observed abundance of species i within the line transect.

Consequently, a simple relationship between the species-specific Moran's I index and the species-specific index  $v_F(i)$  can be established as follows:

$$I_F(i) = \left(\frac{m}{n_i}\right) v_F(i).$$

Accordingly, when conducting line-transect sampling, the functional trait-based conspecific-encounter index  $v_F$  can be computed as the sum of the abundance-weighted Moran's I index for each single species along the line transect as follows:

$$v_F = \sum_{i \in S} \left(\frac{n_i}{m}\right) I_F(i). \tag{A5}$$